## Important Concepts

## Fractions as Parts of a Whole

In the part-whole interpretation of fractions, students should determine what the whole is, divide the whole into equal-size parts (that are not necessarily the same shape), recognize the number of parts they need to represent the situation, and form a fraction by placing the parts needed over the number of parts into which they have divided the whole.

## Fractions as Measures or Quantities

In this interpretation, students think of fractions as numbers.

## Fractions as Decimals

Students need to understand decimals in two ways: as special fractions with denominators of 10 and powers of 10, and as a natural extension of the place-value system for representing quantities less than 1.

## Ratio

Students build understanding of ratios as comparisons of numbers. Students express ratios in different ways: with the language of for every, using the word to, with colon notation ( $a: b$ ), and using the word per.

## Unit Rate

A unit rate is a comparison in which one of the numbers being compared is 1 unit. You can use unit rates to calculate equivalent ratios.

## Rate Table

Rate tables are a way to express equivalent ratios. For example, if you know that 1 ounce of popcorn kernels yields 4 cups of popped corn, you can use a rate table to calculate other amounts.

## Examples

If there are 24 students in the class and 16 are girls, then you can represent the part of the whole that is girls as $\frac{16}{24}$. You can also represent $\frac{16}{24}$ as $\frac{2}{3}$.
The denominator 3 tells into how many equal-size parts the whole has been divided, and the numerator 2 tells how many of the equal-size parts have been shaded.

A fraction can be a measurement that is "in between" two whole measures. Students see this every day in references such as $2 \frac{1}{2}$ brownies or $7 \frac{3}{4}$ inches.

For example, to find the decimal representation of the fraction $\frac{2}{5}$, rewrite it with a power of 10 in the denominator.

$$
\frac{2}{5}=\frac{4}{10}
$$

The fraction has tenths in the denominator, so the decimal equivalent places the 4 in the tenths place.

$$
\frac{4}{10}=0.4
$$

When you say that $\frac{1}{6}$ of a school is sixth graders, strictly speaking, this is not a number but a ratio. It compares a part to the whole: for every 6 students, 1 is a sixth grader.

The ratio of the sixth-grade fundraising goal to the seventh-grade fundraising goal is $60: 90$.
Mary runs at 5 miles per hour.

Finn runs 10 miles in 2 hours.
Finn runs 2.5 miles in a half hour (or 30 minutes).
Finn runs 1 mile in $\frac{1}{5}$ hour (or 12 minutes).
The statement Finn runs 1 mile in 12 minutes expresses a unit rate.

## Cups of Popcorn From Ounces of Kernels

| Number of Cups <br> of Popcorn | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 | 48 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of Ounces <br> of Popcorn Kernels | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |

